

Method 6 explained in Mathcad, by Francois de Villiers:

- Solve gamma (glide angle) using horizontal equilibrium
- Solve V (flight speed) using vertical equilibrium
- Solve Py (calage point) using equilibrium of moments

$$L_w = K_l \cdot \frac{1}{2} \cdot \rho \cdot C_l \cdot V^2 \cdot A \quad \dots 1$$

$$D_w = K_d \cdot \frac{1}{2} \cdot \rho \cdot C_d \cdot V^2 \cdot A \quad \dots\dots 2$$

$$D_p = c_{d_p} \cdot \frac{1}{2} \cdot \rho \cdot V^2 \cdot A_p \quad \dots\dots 3$$

$$D_l = c_{d_{line}} \cdot \left(\frac{1}{2} \cdot \rho \cdot V^2 \right) \cdot A_{line} \quad \dots\dots 4$$

$$L_w \cdot \cos(\gamma) + (D_w + D_l + D_p) \cdot \sin(\gamma) - M_{wing} \cdot g - M_{line} \cdot g - M_{ql} \cdot g - M_{pilot} \cdot g = 0 \quad \dots 5$$

$$-L_w \cdot \sin(q) + (D_w + D_l + D_p) \cdot \cos(q) = 0 \quad \dots\dots 6$$

1 to 4 into 5
$$\frac{V^2 \cdot \rho \cdot \left(A_p \cdot c_{d_p} \cdot \cos(q) + A_{line} \cdot c_{d_{line}} \cdot \cos(q) + A \cdot C_d \cdot K_d \cdot \cos(q) - A \cdot C_l \cdot K_l \cdot \sin(q) \right)}{2} = 0$$

multiply by 2 and divide by V^2 and rho

$$0 = A_p \cdot c_{d_p} \cdot \cos(\gamma) + A_{line} \cdot c_{d_{line}} \cdot \cos(\gamma) + A \cdot C_d \cdot K_d \cdot \cos(\bullet) - A \cdot C_l \cdot K_l \cdot \sin(\gamma)$$

so gamma is not a function of velocity !!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!

solve for γ

$$\gamma := 2 \cdot \operatorname{atan} \left(\frac{\sqrt{A^2 \cdot \textcolor{red}{C}_d^2 \cdot K_d^2 + A^2 \cdot C_l^2 \cdot K_l^2 + 2 \cdot A \cdot A_p \cdot C_d \cdot K_d \cdot c_{d_p} + 2 \cdot A \cdot A_{line} \cdot C_d \cdot K_d \cdot c_{d_{line}} + A_p^2 \cdot c_{d_p}^2 + 2 \cdot A_p \cdot A_{line} \cdot c_{d_p} \cdot c_{d_{line}} + A_{line}^2 \cdot c_{d_{line}}^2 - A \cdot C_l \cdot K_l}}{A_p \cdot c_{d_p} + A_{line} \cdot c_{d_{line}} + A \cdot C_d \cdot K_d} \right)$$

from 5

$$L_w \cdot \cos(\gamma) + (D_w + D_l + D_p) \cdot \sin(\gamma) - M_{wing} \cdot g - M_{line} \cdot g - M_{ql} \cdot g - M_{pilot} \cdot g = 0$$

1 to 4 into 5 and solve for V

$$V := \frac{\sqrt{2 \cdot \sqrt{\rho \cdot g \cdot (M_{ql} + M_{line} + M_{wing} + M_{pilot}) \cdot (A_p \cdot c_{d_p} \cdot \sin(\gamma) + A_{line} \cdot c_{d_{line}} \cdot \sin(\gamma) + A \cdot C_l \cdot K_l \cdot \cos(\gamma) + A \cdot C_d \cdot K_d \cdot \sin(\gamma))}}}{2 \cdot \left(\frac{A_p \cdot \rho \cdot c_{d_p} \cdot \sin(\gamma)}{2} + \frac{A_{line} \cdot \rho \cdot c_{d_{line}} \cdot \sin(\gamma)}{2} + \frac{A \cdot C_l \cdot K_l \cdot \rho \cdot \cos(\gamma)}{2} + \frac{A \cdot C_d \cdot K_d \cdot \rho \cdot \sin(\gamma)}{2} \right)}$$

$$\textcolor{green}{g} := \frac{\frac{g}{m}}{\sec^2}$$

$$C_l := 0.55619$$

$$C_d := 0.03560$$

$$M_{pilot} := 65.9$$

$$M_{wing} := 5$$

$$M_{line} := 0.295$$

$$M_{riser} := 0.050$$

$$M_{ql} := 0.048$$

$$M_t := M_{pilot} + M_{wing} + M_{line} + M_{ql} = 71.243$$

$$\textcolor{green}{A} := 12.4577$$

$$\rho := 1.225$$

$$\textcolor{green}{g} := 9.807$$

$$6 \times 8$$

$$K_l := 1$$

$$K_d := 1.4$$

$$c_{d_{line}} \equiv 1.07857$$

$$A_{line} := 1 \cdot 0.2515$$

$$A_p \equiv 0.4380$$

$$c_{d_p} := 0.6$$

...riser included in lines

$$\gamma := 2 \cdot \operatorname{atan} \left(\frac{\sqrt{A^2 \cdot C_d^2 \cdot K_d^2 + A^2 \cdot C_l^2 \cdot K_l^2 + 2 \cdot A \cdot A_p \cdot C_d \cdot K_d \cdot c_{d_p} + 2 \cdot A \cdot A_{line} \cdot C_d \cdot K_d \cdot c_{d_{line}} + A_p^2 \cdot c_{d_p}^2 + 2 \cdot A_p \cdot A_{line} \cdot c_{d_p} \cdot c_{d_{line}} + A_{line}^2 \cdot c_{d_{line}}^2 - A \cdot C_l \cdot K_l}}{A_p \cdot c_{d_p} + A_{line} \cdot c_{d_{line}} + A \cdot C_d \cdot K_d} \right)$$

$$\gamma = 9.463 \cdot \text{deg}$$

$$V_{\text{ww}} := \frac{\sqrt{2} \cdot \sqrt{\rho \cdot g \cdot (M_{\text{ql}} + M_{\text{line}} + M_{\text{wing}} + M_{\text{pilot}}) \cdot (A_{\text{p}} \cdot \text{cd}_{\text{p}} \cdot \sin(\gamma) + A_{\text{line}} \cdot \text{cd}_{\text{line}} \cdot \sin(\gamma) + A \cdot C_{\text{l}} \cdot K_{\text{l}} \cdot \cos(\gamma) + A \cdot C_{\text{d}} \cdot K_{\text{d}} \cdot \sin(\gamma))}}{2 \cdot \left(\frac{A_{\text{p}} \cdot \rho \cdot \text{cd}_{\text{p}} \cdot \sin(\gamma)}{2} + \frac{A_{\text{line}} \cdot \rho \cdot \text{cd}_{\text{line}} \cdot \sin(\gamma)}{2} + \frac{A \cdot C_{\text{l}} \cdot K_{\text{l}} \cdot \rho \cdot \cos(\gamma)}{2} + \frac{A \cdot C_{\text{d}} \cdot K_{\text{d}} \cdot \rho \cdot \sin(\gamma)}{2} \right)}$$

$$V = 12.743$$

$$W_{\text{w}} := M_{\text{wing}} \cdot g \qquad W_{\text{l}} := M_{\text{line}} \cdot g$$

$$W_{\text{p}} := M_{\text{pilot}} \cdot g$$

$$C_{\text{pz}} := 0.299 \qquad C_{\text{py}} := 0.489$$

$$\begin{array}{ll} G_{\text{y}} := 0.902 & G_{\text{z}} := 0.499 \\ GL_{\text{y}} := 1.003 & GL_{\text{z}} := 2.507 \end{array}$$

$$\alpha := 9.45 \cdot \text{deg}$$

$$\theta := (\gamma - \alpha)$$

$$P_{\text{z}} := 4.770 + 0.2$$

$$P_{\text{z}} = 4.97$$

$$DL_{\text{y}} := 1.0387 \qquad DL_{\text{z}} := 2.1802$$

$$\begin{array}{l} -(C_{\text{py}} - G_{\text{y}}) \cdot W_{\text{w}} \cdot \cos(\theta) - (C_{\text{pz}} - G_{\text{z}}) \cdot W_{\text{w}} \cdot \sin(\theta) \dots = 0 \\ + -(C_{\text{py}} - GL_{\text{y}}) \cdot W_{\text{l}} \cdot \cos(\theta) - (C_{\text{pz}} - GL_{\text{z}}) \cdot W_{\text{l}} \cdot \sin(\theta) \dots \\ + -(C_{\text{py}} - P_{\text{y}}) \cdot W_{\text{p}} \cdot \cos(\theta) - (C_{\text{pz}} - P_{\text{z}}) \cdot W_{\text{p}} \cdot \sin(\theta) \dots \\ + (C_{\text{py}} - DL_{\text{y}}) \cdot D_{\text{l}} \cdot \sin(\alpha) + (C_{\text{pz}} - DL_{\text{z}}) \cdot D_{\text{l}} \cdot \cos(\alpha) \dots \\ + (C_{\text{py}} - P_{\text{y}}) \cdot D_{\text{p}} \cdot \sin(\alpha) + (C_{\text{pz}} - P_{\text{z}}) \cdot D_{\text{p}} \cdot \cos(\alpha) \end{array}$$

$$PP = P_{\text{z}} \cdot \tan(\theta) + P_{\text{y}}$$

$$D_{\text{p}} := \text{cd}_{\text{p}} \cdot \frac{1}{2} \cdot \rho \cdot V^2 \cdot A_{\text{p}}$$

$$L_{\text{w}} := K_{\text{l}} \cdot \frac{1}{2} \cdot \rho \cdot C_{\text{l}} \cdot V^2 \cdot A$$

$$D_{\text{l}} := \text{cd}_{\text{line}} \cdot \left(\frac{1}{2} \cdot \rho \cdot V^2 \right) \cdot A_{\text{line}}$$

$$D_{\text{w}} := K_{\text{d}} \cdot \frac{1}{2} \cdot \rho \cdot C_{\text{d}} \cdot V^2 \cdot A$$

$$P_{\text{y}} := - \frac{W_{\text{w}} \cdot \cos(\theta) \cdot (C_{\text{py}} - G_{\text{y}}) - D_{\text{p}} \cdot \cos(\alpha) \cdot (C_{\text{pz}} - P_{\text{z}}) + W_{\text{l}} \cdot \cos(\theta) \cdot (C_{\text{py}} - GL_{\text{y}}) + W_{\text{w}} \cdot \sin(\theta) \cdot (C_{\text{pz}} - G_{\text{z}}) + W_{\text{l}} \cdot \sin(\theta) \cdot (C_{\text{pz}} - GL_{\text{z}}) + W_{\text{p}} \cdot \sin(\theta) \cdot (C_{\text{pz}} - P_{\text{z}}) - C_{\text{py}} \cdot D_{\text{p}} \cdot \sin(\alpha) - C_{\text{pz}} \cdot D_{\text{p}} \cdot \cos(\alpha)}{D_{\text{p}} \cdot \sin(\alpha) - W_{\text{p}} \cdot \cos(\theta)}$$

$$P_{\text{y}} = 0.723$$

$$\sin(\alpha) + C_{\text{py}} \cdot W_{\text{p}} \cdot \cos(\theta) - D_{\text{l}} \cdot \cos(\alpha) \cdot (C_{\text{pz}} - DL_{\text{z}}) - D_{\text{l}} \cdot \sin(\alpha) \cdot (C_{\text{py}} - DL_{\text{y}})$$

$$PP := (P_{\text{z}} \cdot \tan(\theta) + P_{\text{y}})$$

$$PP = 0.725$$

$$\text{chord}_{\text{center}} := 2.121$$

$$\text{Calage}_{\text{p}} := \frac{P_{\text{y}}}{\text{chord}_{\text{center}}} \cdot 100 = 34.107$$

$$PP_{\text{p}} := \frac{PP}{\text{chord}_{\text{center}}} \cdot 100 = 34.162$$

$$\frac{L_{\text{w}}}{D_{\text{w}}} = 11.1595$$

$$(P_{\text{y}} - C_{\text{py}}) \cdot m = 234.41 \cdot \text{mm}$$

$$(PP - C_{\text{py}}) \cdot m = 235.579 \cdot \text{mm}$$

$$(PP - P_{\text{y}}) \cdot m = 1.169 \cdot \text{mm}$$

$$\frac{L_{\text{w}}}{D_{\text{w}}} = 11.1595$$

$$\frac{L_{\text{w}}}{(D_{\text{w}} + D_{\text{p}} + D_{\text{l}})} = 5.9993$$